BLS signatures, hashing to curves, and more: Dispatches from the IETF

Riad S. Wahby, Dan Boneh

Stanford

August 18th, 2019

People

• BLS signatures authors:

Sergey Gorbunov, Hoeteck Wee, Zhenfei Zhang

- Hash-to-curve authors: Armando Faz-Hernández, Sam Scott, Nick Sullivan, Chris Wood
- Folks whose feedback has been crucial:
 Björn Haase, Dan Harkins, Leo Reyzin,
 Michael Scott, Shoko Yonezawa

The obvious one: interoperability

The obvious one: interoperability

But also: efficiency, security

The obvious one: interoperability



The obvious one: interoperability

But also: efficiency, security Practice "polite crypto" [EWD1300]

→ Do the careful thinking up front so that your users don't have to!

The obvious one: interoperability

But also: efficiency, security Practice "polite crypto" [EWD1300]

→ Do the careful thinking up front so that your users don't have to!

A forcing function for pragmatism
 → Users will ignore bad or confusing standards...

... so make choices (but only the good ones)

1. Standardizing advanced crypto with the IETF

2. BLS signatures, hash-to-curve, and more

Internet Engineering Task Force

"We believe in rough consensus and running code."

Internet Engineering Task Force

"We believe in rough consensus and running code."

Crypto Forum Research Group

"serves as a bridge between theory and practice, bringing new cryptographic techniques to the Internet community"

Internet Engineering Task Force

"We believe in rough consensus and running code."

Crypto Forum Research Group

"serves as a bridge between theory and practice, bringing new cryptographic techniques to the Internet community"

CFRG publishes "Informational" RFCs

→ can be incorporated by "Standards Track" RFCs, e.g., TLS 1.3 incorporates the curve25519 RFC

Internet Engineering Task Force

"We believe in rough consensus and running code."

Crypto Forum Research Group

"serves as a bridge between theory and practice, bringing new cryptographic techniques to the Internet community"

CFRG publishes "Informational" RFCs

→ can be incorporated by "Standards Track" RFCs, e.g., TLS 1.3 incorporates the curve25519 RFC

CFRG has an active mailing list, too!

→ https://irtf.org/cfrg

Per [RFC5743]:

1. CFRG prepares a new "internet draft"

2. IRTF reviews it

3. IESG reviews it

4. RFC Editor prepares and publishes it

Per [RFC5743]:

- 1. CFRG prepares a new "internet draft" technical vetting—correctness
- 2. IRTF reviews it
- 3. IESG reviews it
- 4. RFC Editor prepares and publishes it

Per [RFC5743]:

- 1. CFRG prepares a new "internet draft" technical vetting—correctness
- 2. IRTF reviews it editorial vetting—clarity
- 3. IESG reviews it
- 4. RFC Editor prepares and publishes it

Per [RFC5743]:

1. CFRG prepares a new "internet draft" technical vetting—correctness

2. IRTF reviews it editorial vetting—clarity

3. IESG reviews it

"political" vetting—is CFRG the right group?

4. RFC Editor prepares and publishes it

Per [RFC5743]:

1. CFRG prepares a new "internet draft" technical vetting—correctness

2. IRTF reviews it editorial vetting—clarity

3. IESG reviews it

"political" vetting—is CFRG the right group?

4. RFC Editor prepares and publishes it fine-toothed combing

- 1. Build consensus: the world needs this protocol
 - stakeholders: the community at large (plus CFRG)

- 1. Build consensus: the world needs this protocol
 - stakeholders: the community at large (plus CFRG)
- 2. Write an "individual draft"
 - solicit feedback from stakeholders
 - https://github.com/ietf-gitwg/using-github

- 1. Build consensus: the world needs this protocol
 - stakeholders: the community at large (plus CFRG)
- 2. Write an "individual draft"
 - solicit feedback from stakeholders
 - https://github.com/ietf-gitwg/using-github
- 3. CFRG call for adoption
 - vote on CFRG mailing list: should this group work on this document? who will read and give feedback?

- 1. Build consensus: the world needs this protocol
 - stakeholders: the community at large (plus CFRG)
- 2. Write an "individual draft"
 - solicit feedback from stakeholders
 - https://github.com/ietf-gitwg/using-github
- 3. CFRG call for adoption
 - vote on CFRG mailing list: should this group work on this document? who will read and give feedback?
- 4. edit, implement, present updates at IETF meetings

- 1. Build consensus: the world needs this protocol
 - stakeholders: the community at large (plus CFRG)
- 2. Write an "individual draft"
 - solicit feedback from stakeholders
 - https://github.com/ietf-gitwg/using-github
- 3. CFRG call for adoption
 - vote on CFRG mailing list: should this group work on this document? who will read and give feedback?
- 4. edit, implement, present updates at IETF meetings
- 5. CFRG last call (for objections, comments, etc.)

- 1. Build consensus: the world needs this protocol
 - stakeholders: the community at large (plus CFRG)
- 2. Write an "individual draft"
 - solicit feedback from stakeholders
 - https://github.com/ietf-gitwg/using-github
- 3. CFRG call for adoption
 - vote on CFRG mailing list: should this group work on this document? who will read and give feedback?
- 4. edit, implement, present updates at IETF meetings
- 5. CFRG last call (for objections, comments, etc.)
- 6. hand off document to IRTF, etc.

CFRG standardization process—how long does it take?

Examples (from https://datatracker.ietf.org):

 curve25519/curve448 [RFC7748]: about 1 year 12 drafts in total IRTF, IESG reviews took a few days each RFC Editor queue took 3 months CFRG standardization process—how long does it take?

Examples (from https://datatracker.ietf.org):

- curve25519/curve448 [RFC7748]: about 1 year 12 drafts in total IRTF, IESG reviews took a few days each RFC Editor queue took 3 months
- BLS signatures (WIP): 6 months so far 2 drafts so far
- Hash-to-curve (WIP): 17 months so far 5 drafts so far

There's an RFC for that! [RFC8179]

If you own a patent, you *must* disclose it.

If you know of a patent, you should disclose it.

There's an RFC for that! [RFC8179]

If you own a patent, you *must* disclose it.

- If you know of a patent, you should disclose it.
- → IETF will ask rights holders for written assurance that patents will be licensed to implementors.

There's an RFC for that! [RFC8179]

If you own a patent, you *must* disclose it.

- If you know of a patent, you should disclose it.
- → IETF will ask rights holders for written assurance that patents will be licensed to implementors.

IETF Security Area won't specify "must-implement" protocols that have royalty encumbrances.

There's an RFC for that! [RFC8179]

If you own a patent, you *must* disclose it.

- If you know of a patent, you should disclose it.
- → IETF will ask rights holders for written assurance that patents will be licensed to implementors.

IETF Security Area won't specify "must-implement" protocols that have royalty encumbrances.

Royalty-free "RAND-z" licenses are OK; commitments not to assert patents are better; unencumbered technologies are best.

There's an RFC for that! [RFC8179]

If you own a patent, you *must* disclose it.

- If you know of a patent, you should disclose it.
- → IETF will ask rights holders for written assurance that patents will be licensed to implementors.

IETF Security Area won't specify "must-implement" protocols that have royalty encumbrances.

Royalty-free "RAND-z" licenses are OK; commitments not to assert patents are better; unencumbered technologies are best.

→ Don't patent crypto.

1. Standardizing advanced crypto with the IETF

2. BLS signatures, hash-to-curve, and more











- G₁ ⊆ E₁(𝔽₁) and G₂ ⊆ E₂(𝔽₂) of prime order q generated by P₁ and P₂, respectively
- \mathbb{G}_T of prime order q

- G₁ ⊆ E₁(𝔽₁) and G₂ ⊆ E₂(𝔽₂) of prime order q generated by P₁ and P₂, respectively
- \mathbb{G}_T of prime order q
- $e: \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$, a bilinear map:

$$e(P_1^lpha,P_2^eta)=e(P_1,P_2)^{lpha\cdoteta}\qquad lpha,eta\in\mathbb{Z}_q$$

A pairing-friendly elliptic curve defines:

- G₁ ⊆ E₁(𝔽₁) and G₂ ⊆ E₂(𝔽₂) of prime order q generated by P₁ and P₂, respectively
- \mathbb{G}_T of prime order q

•
$$e: \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$$
, a bilinear map:

$$e(P_1^lpha,P_2^eta)=e(P_1,P_2)^{lpha\cdoteta}\qquad lpha,eta\in\mathbb{Z}_q$$

→ What else might the spec cover?

- G₁ ⊆ E₁(𝔽₁) and G₂ ⊆ E₂(𝔽₂) of prime order q generated by P₁ and P₂, respectively
- \mathbb{G}_T of prime order q

•
$$e: \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$$
, a bilinear map:

$$e(P_1^lpha,P_2^eta)=e(P_1,P_2)^{lpha\cdoteta}\qquad lpha,eta\in\mathbb{Z}_q$$

- → What else might the spec cover?
 - serialization / deserialization

- G₁ ⊆ E₁(𝔽₁) and G₂ ⊆ E₂(𝔽₂) of prime order q generated by P₁ and P₂, respectively
- \mathbb{G}_T of prime order q

•
$$e: \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$$
, a bilinear map:

$$e(P_1^lpha,P_2^eta)=e(P_1,P_2)^{lpha\cdoteta}\qquad lpha,eta\in\mathbb{Z}_q$$

- → What else might the spec cover?
 - serialization / deserialization
 - fast subgroup checks [Bowe19]

- G₁ ⊆ E₁(𝔽₁) and G₂ ⊆ E₂(𝔽₂) of prime order q generated by P₁ and P₂, respectively
- \mathbb{G}_T of prime order q

•
$$e: \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$$
, a bilinear map:

$$e(P_1^lpha,P_2^eta)=e(P_1,P_2)^{lpha\cdoteta}\qquad lpha,eta\in\mathbb{Z}_q$$

- → What else might the spec cover?
 - serialization / deserialization
 - fast subgroup checks [Bowe19]
 - test vectors

 $\mathsf{HashToField}_i: \{0,1\}^* \to \mathbb{F}$

a family of independent ROs indexed by i

HashToField_i : $\{0, 1\}^* \to \mathbb{F}$ a family of independent ROs indexed by *i* MapToCurve : $\mathbb{F} \to E(\mathbb{F})$ [SvdW06,U07,Ica09,BCIMRT10,BHKL13,WB19]

HashToField_i : $\{0, 1\}^* \to \mathbb{F}$ a family of independent ROs indexed by *i* MapToCurve : $\mathbb{F} \to E(\mathbb{F})$ [SvdW06,U07,Ica09,BCIMRT10,BHKL13,WB19] ClearCofactor : $E(\mathbb{F}) \to \mathbb{G}$ [SBCDK09,FKR11,BP18]

HashToField_i : $\{0, 1\}^* \to \mathbb{F}$ a family of independent ROs indexed by *i* MapToCurve : $\mathbb{F} \to E(\mathbb{F})$ [SvdW06,U07,Ica09,BCIMRT10,BHKL13,WB19] ClearCofactor : $E(\mathbb{F}) \to \mathbb{G}$ [SBCDK09,FKR11,BP18]

- $\begin{array}{ll} H(\mathsf{msg}) \to \mathbb{G} & [\mathsf{BCIMRT10},\mathsf{FFSTV13}] \\ Q_1 = \mathsf{MapToCurve}(\mathsf{HashToField}_1(\mathsf{msg})) \\ Q_2 = \mathsf{MapToCurve}(\mathsf{HashToField}_2(\mathsf{msg})) \\ & \mathsf{output ClearCofactor}(Q_1 \cdot Q_2) \end{array}$
 - is indifferentiable from a random oracle to $\ensuremath{\mathbb{G}}$

HashToField_i : $\{0, 1\}^* \to \mathbb{F}$ a family of independent ROs indexed by *i* MapToCurve : $\mathbb{F} \to E(\mathbb{F})$ [SvdW06,U07,Ica09,BCIMRT10,BHKL13,WB19] ClearCofactor : $E(\mathbb{F}) \to \mathbb{G}$ [SBCDK09,FKR11,BP18]

 $\begin{array}{ll} H(\mathsf{msg}) \to \mathbb{G} & [\mathsf{BCIMRT10},\mathsf{FFSTV13}] \\ Q_1 = \mathsf{MapToCurve}(\mathsf{HashToField}_1(\mathsf{msg})) \\ Q_2 = \mathsf{MapToCurve}(\mathsf{HashToField}_2(\mathsf{msg})) \\ & \mathsf{output ClearCofactor}(Q_1 \cdot Q_2) \end{array}$

is indifferentiable from a random oracle to $\ensuremath{\mathbb{G}}$

$\mathsf{KeyGen}() \to (pk, sk): x \stackrel{\scriptscriptstyle \mathbb{R}}{\leftarrow} \mathbb{Z}_q; \text{ output } (P_2^x, x).$

 $\mathsf{KeyGen}() \to (pk, sk): x \xleftarrow{\mathbb{R}} \mathbb{Z}_q; \text{ output } (P_2^x, x).$

 $\operatorname{Sign}(sk, \operatorname{msg}) \to \operatorname{sig:}$ output $H(\operatorname{msg})^{sk} \in \mathbb{G}_1$.

 $\mathsf{KeyGen}() \to (pk, sk): x \xleftarrow{\mathbb{R}} \mathbb{Z}_q; \text{ output } (P_2^x, x).$

 $\operatorname{Sign}(sk, \operatorname{msg}) \to \operatorname{sig:}$ output $H(\operatorname{msg})^{sk} \in \mathbb{G}_1$.

Verify $(pk, msg, sig) \rightarrow {OK, \bot}$: if $e(H(msg), pk) = e(sig, P_2)$, output OK, else output \bot .

 $\mathsf{KeyGen}() \to (pk, sk): x \xleftarrow{\mathbb{R}} \mathbb{Z}_q; \text{ output } (P_2^x, x).$

 $\operatorname{Sign}(sk, \operatorname{msg}) \to \operatorname{sig:}$ output $H(\operatorname{msg})^{sk} \in \mathbb{G}_1$.

Verify $(pk, msg, sig) \rightarrow {OK, \bot}$: if $e(H(msg), pk) = e(sig, P_2)$, output OK, else output \bot .

$$e(H(\mathrm{msg}), P_2^{\mathrm{x}}) = e(H(\mathrm{msg})^{\mathrm{x}}, P_2)$$

$$\mathsf{KeyGen}() \to (pk, sk): x \xleftarrow{\mathbb{R}} \mathbb{Z}_q; \mathsf{output} \ (P_2^x, x).$$

 $\operatorname{Sign}(sk, \operatorname{msg}) \to \operatorname{sig:} \operatorname{output} H(\operatorname{msg})^{sk} \in \mathbb{G}_1.$

Verify $(pk, msg, sig) \rightarrow {OK, \bot}$: if $e(H(msg), pk) = e(sig, P_2)$, output OK, else output \bot .

$$e(H(\mathrm{msg}), P_2^{\mathrm{x}}) = e(H(\mathrm{msg})^{\mathrm{x}}, P_2)$$

KeyGen()
$$\rightarrow$$
 (pk, sk) $x \leftarrow^{\mathbb{R}} \mathbb{Z}_q$; output (P_2^x, x) .
Sign $(sk, msg) \rightarrow$ sig: output $H(msg)^{sk} \in \mathbb{G}_1$.

Verify(pk, msg, sig) \rightarrow {OK, \perp }: if $e(H(msg), pk) = e(sig, P_2)$, output OK, else output \perp .

$$e(H(\mathrm{msg}), P_2^x) = e(H(\mathrm{msg})^x, P_2)$$

 $\begin{array}{l} \mathsf{Aggregate}(\mathsf{sig}_1, \ldots, \mathsf{sig}_n) \to \mathsf{sig}:\\ \mathsf{output} \prod_i \mathsf{sig}_i \in \mathbb{G}_1. \end{array}$

 $\begin{array}{l} \mathsf{Aggregate}(\mathsf{sig}_1, \dots, \mathsf{sig}_n) \to \mathsf{sig}:\\ \mathsf{output} \prod_i \mathsf{sig}_i \in \mathbb{G}_1. \end{array}$

VerMulti $(pk_1, ..., pk_n, msg, sig) \rightarrow \{OK, \bot\}$: if $e(H(msg), \prod_i pk_i) = e(sig, P_2)$, output OK, else output \bot .

 $\begin{array}{l} \mathsf{Aggregate}(\mathsf{sig}_1, \dots, \mathsf{sig}_n) \to \mathsf{sig}:\\ \mathsf{output} \prod_i \mathsf{sig}_i \in \mathbb{G}_1. \end{array}$

VerMulti $(pk_1, ..., pk_n, msg, sig) \rightarrow \{OK, \bot\}$: if $e(H(msg), \prod_i pk_i) = e(sig, P_2)$, output OK, else output \bot .

VerBatch(pk_1 , msg₁, ..., pk_n , msg_n, sig) \rightarrow {OK, \perp }: if $\prod_i e(H(msg_i), pk_i) = e(sig, P_2)$, output OK, else output \perp .

Aggregate(sig₁, ..., sig_n) \rightarrow sig: output $\prod_i sig_i \in \mathbb{G}_1$.

VerMulti $(pk_1, ..., pk_n, msg, sig) \rightarrow {OK, \bot}:$ if $e(H(msg), \prod_i pk_i) = e(sig, P_2)$, output OK, else output \bot .

VerBatch($pk_1, msg_1, ..., pk_n, msg_n, sig$) \rightarrow {OK, \perp }: if $\prod_i e(H(msg_i), pk_i) = e(sig, P_2)$, output OK, else output \perp . Rogue key attack

Let's say Alice has pk_a and Bob has pk_b .

Mallory samples $x \leftarrow^{\mathbb{R}} \mathbb{Z}_q$ and computes

$$pk_m = P_2^{\scriptscriptstyle X} \cdot (pk_a \cdot pk_b)^{-1}$$

Rogue key attack

Let's say Alice has pk_a and Bob has pk_b .

Mallory samples $x \stackrel{\scriptscriptstyle \mathbb{R}}{\leftarrow} \mathbb{Z}_q$ and computes

$$pk_m = P_2^{\scriptscriptstyle X} \cdot (pk_a \cdot pk_b)^{-1}$$

Since $\prod pk_i = P_2^x$, Mallory can forge a multi-signature for any msg:

$$e(H(\mathsf{msg}),\prod pk_i)=e(H(\mathsf{msg})^{ imes},P_2)$$

Defending against rogue keys Require unique messages [BGLS03]: But: no fast multi-sig verification.

Require unique messages [BGLS03]: But: no fast multi-sig verification.

Message augmentation [BGLS03,BNN07]: Sign *pk* || msg, ensuring uniqueness (so: no fast multi-sig verification).

Require unique messages [BGLS03]: But: no fast multi-sig verification.

Message augmentation [BGLS03,BNN07]: Sign *pk* || msg, ensuring uniqueness (so: no fast multi-sig verification).

Proof of possession [Bol03,LOSSW06,RY07]: Require key owners to furnish Sign(*sk*, *pk*) (gives fast multi-sig verification).

Require unique messages [BGLS03]: But: no fast multi-sig verification.

Message augmentation [BGLS03,BNN07]: Sign *pk* || msg, ensuring uniqueness (so: no fast multi-sig verification).

Proof of possession [Bol03,LOSSW06,RY07]: Require key owners to furnish Sign(*sk*, *pk*) (gives fast multi-sig verification).

Random linear combination [BDN18]: Check $e(H(msg_i), \prod_i pk_i^{\alpha_i}) \stackrel{?}{=} e(\prod_i sig_i^{\alpha_i}, P_2)$ for pseudorandomly-generated α_i .

Require unique messages [BGLS03]: But: no fast multi-sig verification.

Message augmentation [BGLS03,BNN07]: Sign *pk* || msg, ensuring uniqueness (so: no fast multi-sig verification).

Proof of possession [Bol03,LOSSW06,RY07]: Require key owners to furnish Sign(*sk*, *pk*) (gives fast multi-sig verification).

Random linear combination [BDN18]: Check $e(H(msg_i), \prod_i pk_i^{\alpha_i}) \stackrel{?}{=} e(\prod_i sig_i^{\alpha_i}, P_2)$ for pseudorandomly-generated α_i .

✓ Make things hard to break, but add firewalls for when they do.

- ✓ Make things hard to break, but add firewalls for when they do.
- Implement, implement, implement: that's what the standard is for!

- ✓ Make things hard to break, but add firewalls for when they do.
- Implement, implement, implement: that's what the standard is for!
- You can't make everyone happy (but don't take it personally).

- ✓ Make things hard to break, but add firewalls for when they do.
- Implement, implement, implement: that's what the standard is for!
- You can't make everyone happy (but don't take it personally).
- ✓ The IETF is a great place for new crypto!

- ✓ Make things hard to break, but add firewalls for when they do.
- Implement, implement, implement: that's what the standard is for!
- You can't make everyone happy (but don't take it personally).
- ✓ The IETF is a great place for new crypto!

https://github.com/cfrg/draft-irtf-cfrg-bls-signature https://github.com/cfrg/draft-irtf-cfrg-hash-to-curve https://bls-hash.crypto.fyi